

# Study of Thermodynamic Parameter and Elastic Constants in Lead Chalcogenides

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## ABSTRACT

*In the present paper, we have been studied the elastic constants of lead chalcogenides [(PbX, X= Se and Te)] with help of lattice constants. The elastic constant such as Young's modulus, bulk modulus, shear modulus and Poisson ratio in lead chalcogenides [(PbX, X= Se and Te)] are calculated. The calculated values are a close agreement with the experimental results.*

**Keywords:** Lead chalcogenides, lattice constant, Elastic constant.

## I. INTRODUCTION

The Mechanical properties of PbSe and PbTe are shown the n-type and p-type semiconductor in the NaCl Structure. The PbSe and PbTe are used in thermoelectric devices due to their brittle nature. They have unique structural and electronic properties. They have wide technological applications and used to fabricate in various optoelectronic, spintronic, thermo- electronic devices, nanoscience, nanotechnology [1-9]. The lead chalcogenides (Pb X, X=Se and Te) are narrow band gap (0.2-0.4 eV) semiconductors at lower temperature. The theoretical and experimental studies have been performed on their mechanical properties and typically has a lower hardness [10-17]. Those properties have been explained in terms of elastic constant [17]. The elastic constant such as Young's moduli (Y), bulk moduli (B), shear moduli (G) and Poisson ratio ( $\sigma$ ) in lead chalcogenides [(PbX, X= Se and Te)] are calculated with help of lattice constants and using the Reuss-Voigt-Hill method [18-20]. The calculated values are close agreement with the experimental results.

## 2. THEORETICAL CALCULATION

The elements selenium, and tellurium are called chalcogens and their compounds are referred as chalcogenides. The crystal structure of lead chalcogenide is NaCl (B1) type. The coordination number and bond between lead (Pb) and chalcogen {X= Se, Te} are 6 and ionic respectively. The mechanical properties were studied in terms of lattice constant and Reuss-Voigt-Hill method [18-20]. Various experimental studies have been found the lead chalcogenides exhibit strongly anharmonic lattice dynamics [21]. The thermodynamics the enthalpy in NaCl (B1) structure is given by

$$H=E+PV \quad (1)$$

The Gibbs free energy is given by

$$G=H-TS \quad (2)$$

According to the Classical Heisenberg Model, the Hamiltonian is given by

$$\mathcal{H} = -\frac{1}{2} \sum_i \vec{S}_i (J_1 \sum_j^{nn} \vec{S}_j + J_2 \sum_j^{nnn} \vec{S}_j) \quad (3)$$

With normalized spin vectors  $\vec{S}_i$  and  $\vec{S}_j$  and where summation over nearest neighbor and next nearest neighbor.

The energy differences in term of  $J_1$  and  $J_2$  are given the following relation,

$$\Delta E_1 = 8J_1$$

$$\Delta E_2 = 6J_1 + 6J_2$$

The enthalpy of lead chalcogenide crystal is defined as

$$H \approx H_{ELEC} + H_{VIB}^0 + H_{VIB}(T) + H_{ROT}(T) + H_{TRANS}(T) + RT \quad (4)$$

where,  $H_{ELEC}$  be the electronic component of enthalpy,  $H_{VIB}^0$  be the vibrational component of enthalpy (main State),  $H_{VIB}(T)$  be the vibrational component of enthalpy,  $H_{ROT}(T)$  be the rotational component of enthalpy,  $H_{TRANS}(T)$  be the trans. component of enthalpy,  $R$  be the universal gas constant and  $T$  be the temperature.

The entropy of the crystal is the sum of following component ,

$$\Delta S = S_{TRANS} + S_{VIB} + S_{ELECT} - nR[\ln(nN_0) - 1] \quad (5)$$

Where,  $N_0$  be the Avogadro constant and  $N$  be the number of moles in molecules.

The Gibbs free energy of the crystal in term entropy of individual members of molecules reagent Pb and X=(Se and Te) then,

$$\Delta G = H_{Pb} - H_X + \frac{1}{2} \sum_{i \in Pb} h \nu_i - \frac{1}{2} \sum_{j \in X} h \nu_j - T (S_{VIB}^{Pb} - S_{VIB}^X + S_{ROT}^{Pb} - S_{ROT}^X + S_{TRANS}^{Pb} - S_{TRANS}^X) \quad (6)$$

Where,  $H_{Pb}$  be the enthalpy of lead,  $H_X$  be the enthalpy of chalcogen[X=Se and Te],  $S_{VIB}^{Pb}$  be the entropy of lead due to vib. component,  $S_{VIB}^X$  be the entropy of chalcogen due to vib. component,  $S_{ROT}^{Pb}$  be the entropy of lead due to rot. component,  $S_{ROT}^X$  be the entropy of chalcogen due to rot. component,  $S_{TRANS}^{Pb}$  be the entropy of lead due to trans. Component and  $S_{TRANS}^X$  be the entropy of chalcogen due to trans. component.

The mechanical properties in term of elastic constant such as bulk modulus (B) is given by

$$B = \frac{1}{3} (c_{11} + 2 c_{12}) \quad (7)$$

Where,  $c_{11}$ , and  $c_{12}$  are elastic constants.

The value of Poisson ratio is given by

$$\sigma = \frac{3B-2G}{2(3B-G)} \quad (8)$$

where ,B be the bulk modulus, G be the average shear modulus and  $\bar{G}$  be the arithmetic mean of Voigt  $G_v$ , and Reuss  $G_R$ ,

Those values are expressed in term of elastic constants ( $c_{11}, c_{12}$  and  $c_{44}$  ) are given by

$$G_v = \frac{1}{5} (c_{11} - c_{12} + 3c_{44}) \quad (9)$$

$$G_R = \frac{5(c_{11}-c_{12})c_{44}}{3(c_{11}-c_{12})+4c_{44}} \quad (10)$$

The value of Young's modulus in term of bulk modulus and shear modulus is given by

$$Y = \frac{9BG}{3B+G} \quad (11)$$

The calculated values of Young's moduli (Y),bulk moduli(B),shear moduli(G) and Poisson ratio ( $\sigma$ ) in lead chalcogenides (PbX, X= Se and Te) are listed in table 1. and table 2. Our calculated values are close agreement with the experimental results.

### 3. CONCLUSIONS

The objective of the study was to understand some of thermodynamic parameter and elastic constants with help of lattice constants. In this paper, we have studied and analyzed the mechanical properties such as Young's modulus (Y),bulk modulus

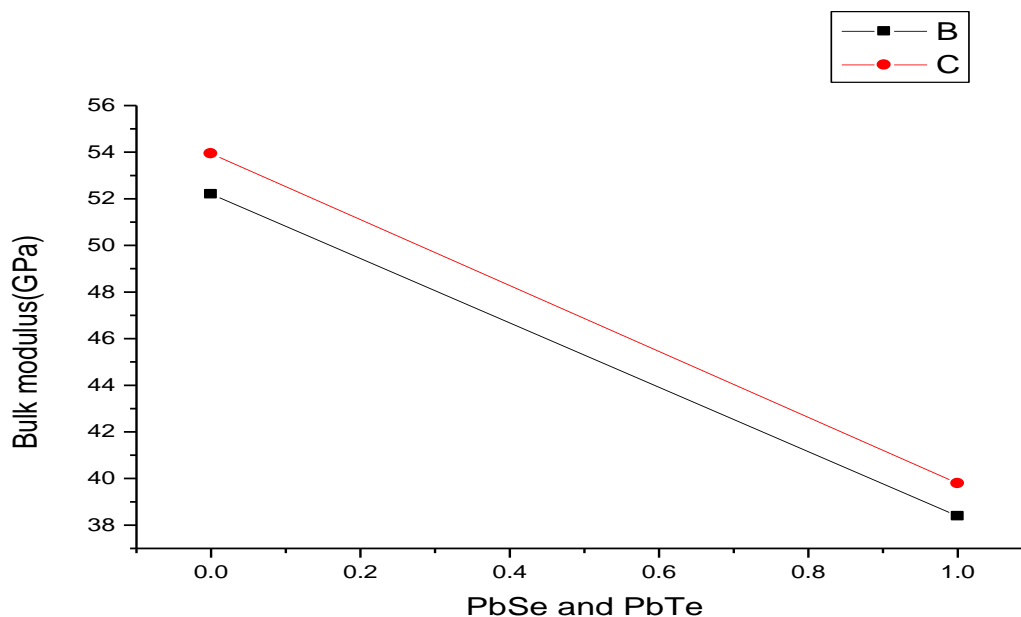
(B),shear modulus (G) and Poisson ratio ( $\sigma$ ) in lead chalcogenides [(PbX, X= Se and Te)] with help of lattice constants and Reuss-Voigt-Hill method.Our calculated values of lattice constants are predicted in table 1.and table 2.The graph plotted between bulk modulus versus PbSe and PbTe is shown in fig1.Another graph predicted Young’s modulus versus PbSe and PbTe (chalcogenide Compound) in fig 2.Finally,our calculated values of elastic constants are close agreement with experimental result.

**Table 1.The values of lattice constant and bulk modulus (B) for lead chalcogenide [(PbX, X= Se and Te)]**

Compound	$c_{11}$	$c_{12}$	$c_{44}$	Bulk modulus(B) GPa Exp.[22-23]	Bulk modulus(B) GPa Calc.
PbSe	123.75	19.34	15.92	52.2	53.94
PbTe	105.32	7.02	13.22	38.39	39.79

**Table 2. The values of Young’s modulus (Y) , shear modulus (G) and Poisson ratio for lead chalcogenide [(PbX, X= Se and Te)]**

compound	Young’s modulus(Y) GPa Exp . [22-23]	Young’s Modulus (Y) GPa Calc.	Shear modulus(G)GPa a Exp. [22-23]	Shear Modulus(G) GPa Calc.	Poisson ratio ( $\sigma$ ) Exp. [22-23]	Poisson ratio ( $\sigma$ ) Calc.
PbSe	57.65	67.73	21.9	26.24	0.315	0.290
PbTe	58.05	48.83	22.95	18.85	0.264	0.296



**Fig.1. Bulk modulus for PbSe and PbTe**

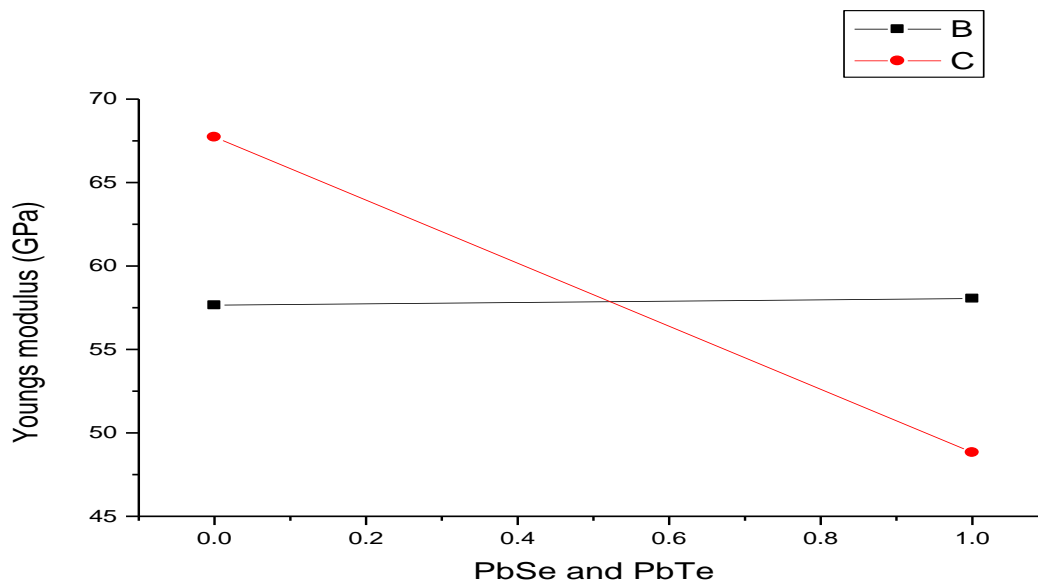


Fig.2.Young's modulus for PbSe and PbTe

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