



# NON-LINEAR CONTACT STRESS ANALYSIS OF L P COMPRESSOR BLADE-DISC ASSEMBLY FOR GAS AND CENTRIFUGAL LOAD

Bheemagonda <sup>[1]</sup> and Anand S.N <sup>[2]</sup>

<sup>1</sup> PG Student, <sup>2</sup> Associate professor

*School of Mechanical Engineering, REVA UNIVERSITY,*

*Bangalore, Karnataka, India*

## ABSTRACT

*Modern military aero engines set very high technology standards for the component design, as they operate in an increasingly hostile thermo-mechanical environment. With rapid advancement in materials, manufacturing processes and analytical tools, there is an increase in demands on the aero engine performance and thrust-to-weight ratio. The rotary parts like blades, disks, shafts of compressor or turbine have taken into very important consideration in gas turbine engines. As they are subjected to very high centrifugal loads and gas loads.*

*In the present work, finite element analysis of typical conventional compressors bladed disc assembly has been carried out to study the stress levels at critical locations in discussing standard commercial finite element software (ANSYS 10.0). Conventional bladed disc's assembly are already operating at high stress level, because of high speed and thermal gradients across the disc bore and rim, weight optimization of disc is possible only by resorting to other techniques. A significant part of the disk weight is at blade attachment region, because the additional disk material required withstanding the centrifugal pull of the blade, an attempt has been made to find the contact stress for the weight optimized compressor bladed disc assembly.*

*Determination of yield strength and effective comparison with the input yield strength has been done. This observation clearly shows that compressor blade and disk are in safe position from the crack initiation.*

*The peak values of compressive stresses also induced near the region of contact stresses are also well within the design limit. The peak value of von-misses stresses induced near the region of contact stresses are also well within the design limit.*

**Keywords:** *Aero Engine, Finite Element Analysis, Gas Turbine Engines, Thermo-Mechanical Environment, Stress Analysis.*

## 1. INTRODUCTION

The stress analysis of the dovetail or the derivative fir-tree root type of turbine blade fixing has received the attention of several experimental investigators employing the techniques of photo elasticity since the introduction of this method as a general stress analysis tool. The emphasis of these investigations however has been on the stress values on the unloaded boundaries of the component, particular attention having been paid to the fillet radius at the

junction of the dovetail and the radial shank of the blade. Consideration of the failures occurring in practice however suggests that the fillet region is not always the site for fatigue cracks and that the region below and adjacent to the contacting flanks of the joint is just as likely to provide a site for crack initiation.

A requirement to obtain internal stress distributions leads the experimental stress analysis to the photo elastic method and the theoretical stress analysis now a days to the finite element or boundary element methods of numerical analysis. It was decided that it would be interesting to compare the photo elastic results for this problem with those obtained from using a commercially available finite element package.

## 2. MATERIALS

### 2.1 BLADE MATERIAL

The materials that have found to be suitable for use in blades are steels, titanium alloys and nickel-based alloys. All the three types of alloys, which are mainly used, have varying proportion of chromium and aluminum to improve the strength and corrosion at high temperature. Titanium alloys are preferred to steel because of its lower density (nearly 50%). Titanium has superior oxidation resistance.

### 2.1 DISC MATERIAL

Disc carries a series of blades, so great care must be taken in design and material selection to avoid the catastrophic failure, based on yield and ultimate strength at approaching temperatures, resistance to creep relaxation and good fracture toughness at ambient temperature conditions as well as operating temperatures. For blisk, Titanium based alloy (Ti-64) is used.

## 3. Methodology: Geometric modelling of Compressor Rotor Blade and Disc

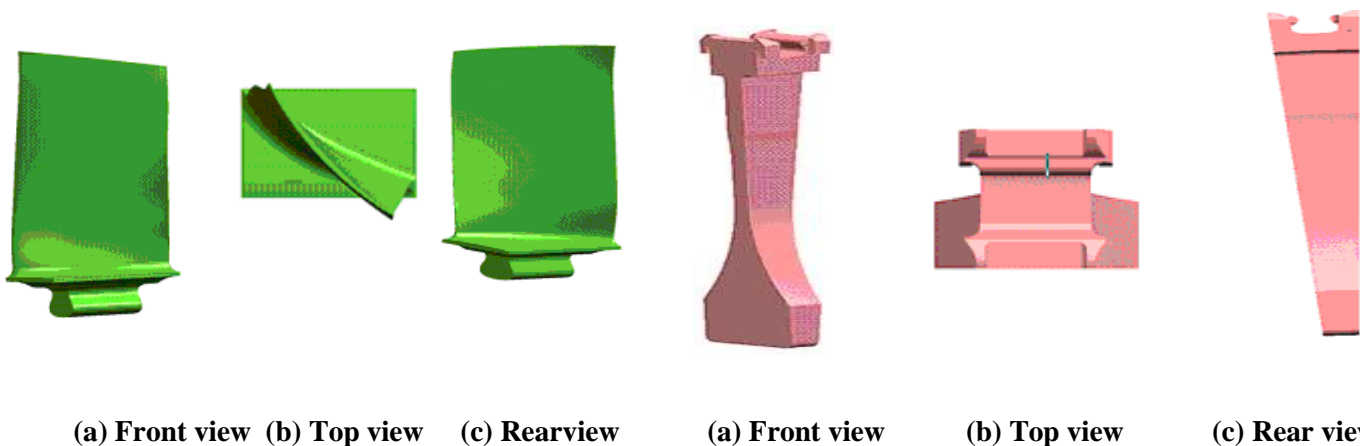


Fig. 3.1 Aero engine compressor rotor blade

Fig. 3.3 Aero engine compressor rotor Disc

### 3.4 Compressor blade disc assembly

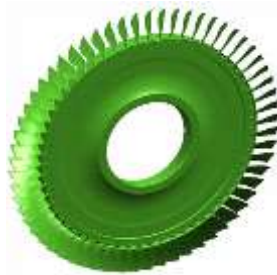


Fig.3.4 Aero engine compressor rotor Assembly

### 3.5 MATERIAL PROPERTIES

Table1. Material property.

Material Properties		Ti-64Al-4V	
Physical Properties		Value	Units
Density		4.43E+03	Kg/m <sup>3</sup>
Mechanical Properties			
Modulus of Elasticity		1.14E+05	Mpa
Compressive Strength	Yield	970	Mpa
Poisson's Ratio		.342	
Fatigue Strength		240	Mpa

### 4. Boundary conditions

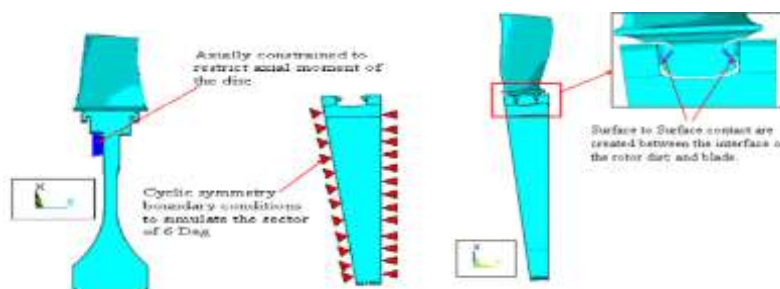
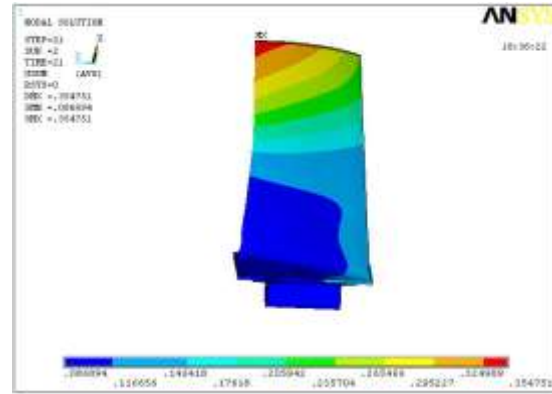
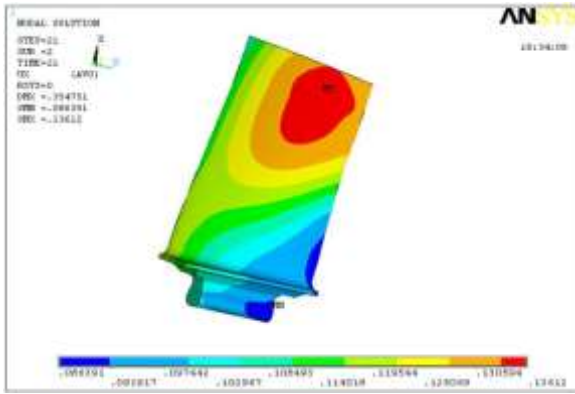


Fig.4.1 Boundary condition for the analysis of the Disc Fig.4.2 Boundary condition for the Contact analysis

### 5. Results and Analysis

Displacement distribution results in the ROTOR BLADE

Deflections are in mm



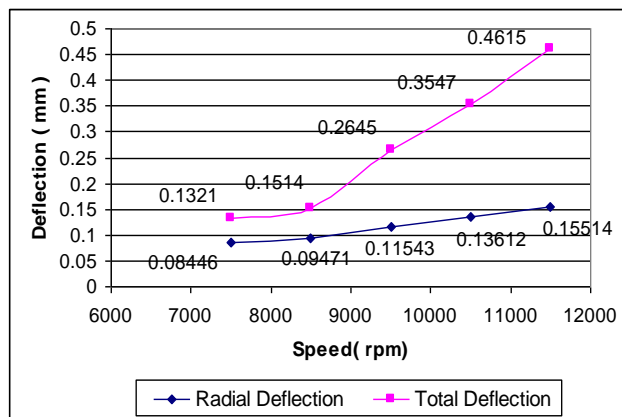
**Fig 5.1 Radial Deflection along X-direction of a Rotor Blade      Fig 5.2 Total Deflection of Rotor Blade**

Fig 5.1 shows that radial deflection along X-direction which signification is that the radial clearance between compressor blade and casing (0.134mm) compared to the existing standard value of clearance (0.5mm) by analyzing the deformation distribution in the compressor blade and disk assembly. Whenever deflection starts radial clearance between compressor blade and casing reduce.

The main observation is that analyzing deflection from Table 5.1 and Fig 5.3, The Optimum value of Radial and Total deflection is well below the standard value, so whole compressor is safe from the radial deflection in compressor blade. If exceed the standard value, again repeat the same analysis by having different loads. The following Table 5.1 and Fig 5.3 shows the variation of Radial as well as Total Deflection for various Centrifugal Loads.

**Table.5.1 Deflections in Blade due to varying Speeds**

Speed (rpm)	Radial Deflection (mm)	Total Deflection (mm)
7500	0.08446	0.1321
8500	0.09471	0.1514
9500	0.11543	0.2645
10500	0.13612	0.3547
11500	0.15514	0.4615



**Fig.5.3 Variation of Radial and Total Deflection of Blade due to Varying Speeds**

## 5.2 Typical stress distribution results in the ROTOR BLADE

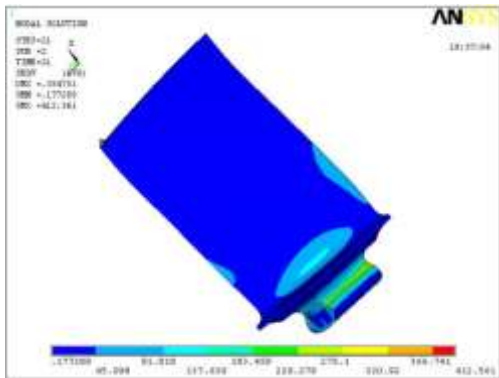


Fig 5.4 Equivalent stress distribution in rotor blade

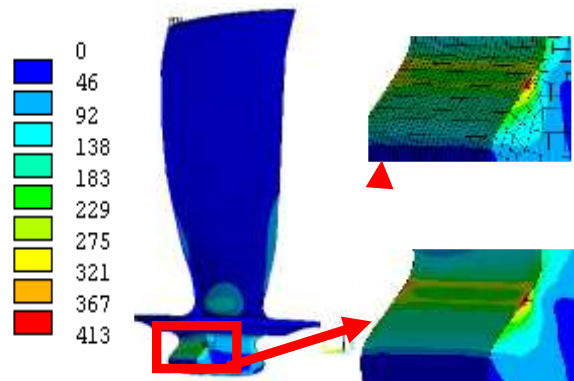


Fig 5.5 Equivalent stress distribution in rotor blade with mesh

### 1<sup>st</sup> Principle Stress

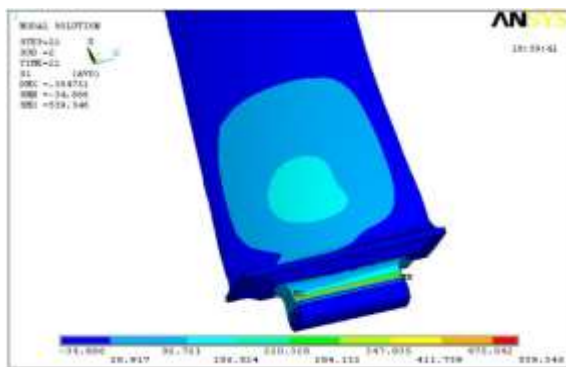


Fig 5.6 First Principle stress of a Rotor Blade along x-direction

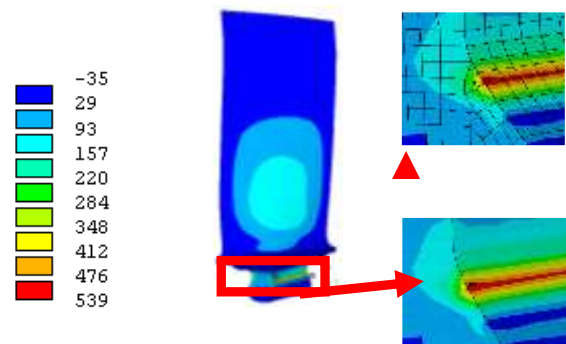


Fig5.7 First principle stress of a Rotor Blade X-direction with mesh

From the analysis of the compressor blade maximum stresses are induced due to existence of contact between compressor blade roots and dovetail groove of the disc in a running speed of 10500rpm. The main observations from the analysis are Equivalent stresses and 1st Principle Stresses are effectively compared with the standard material yield strength (970mpa, material property). The yield strength means stress at which the plastic deformation takes place after the elastic limit. If it exceeds the standard value then there may be chances of fracture initiation at the contact position. But observation clearly shows that the value is within the design limit so, compressor blade and disc assembly are in safe position from the crack initiation (breaking point) at 10500rpm. But when the speed increased to 11500rpm we can notice the reduce in the stress by fig.6.8 which indicates the initiation of crack at the contact region

Table.5.2 Stresses in Blade due to varying Speeds

Speed (rpm)	1 <sup>st</sup> Principle Stress (Mpa)	Equivalent Stress(Mpa)
7500	399.66	311.112
8500	422.45	356.66
9500	498.59	391.22
10500	539.346	412.561
11500	510.79	398.62

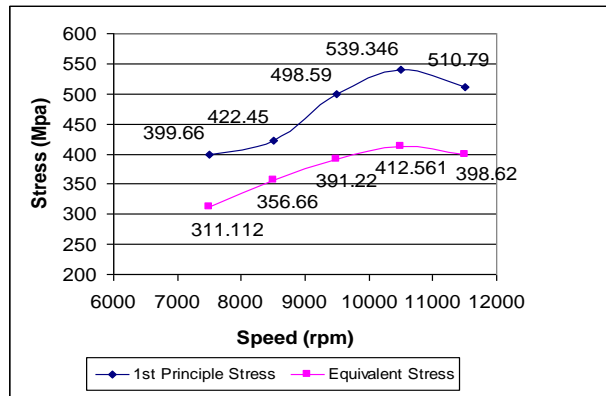


Fig.5.8 Variation of Stresses in Blade due to varying speeds

### 5.3 Typical deformation distribution in compressor disc

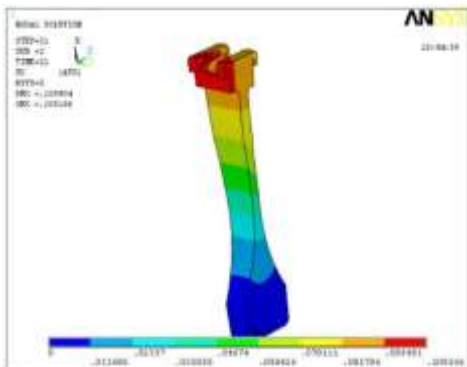


Fig.5.9 Deformation distribution along UX

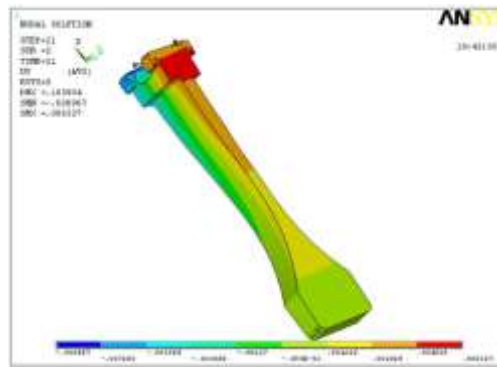


Fig.5.10 Deformation distribution along UY

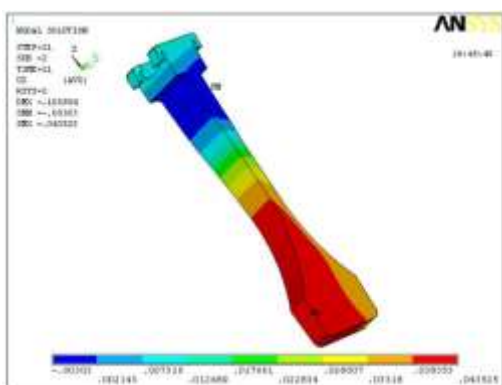


Fig.5.11 Deformation distribution along UZ

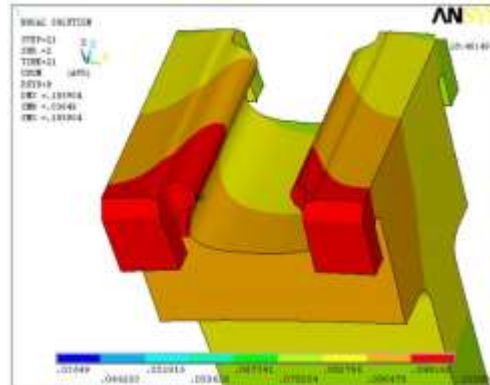
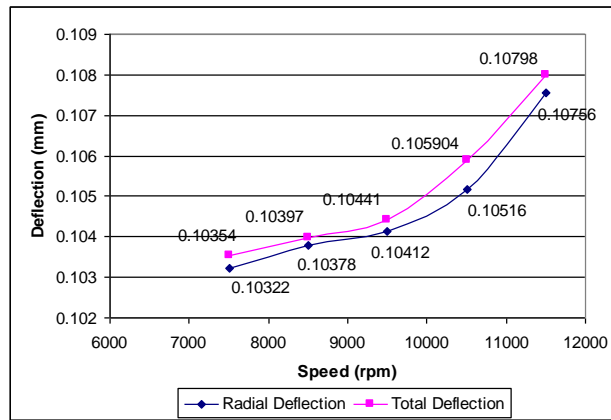


Fig.5.12 Deformation distribution along USUM

**Table.5.3 Deflections in Disc due to varying Speeds**

Speed (rpm)	Radial Deflection (mm)	Total Deflection (mm)
7500	0.10322	0.10354
8500	0.10378	0.10397
9500	0.10412	0.10441
10500	0.10516	0.105904
11500	0.10756	0.10798



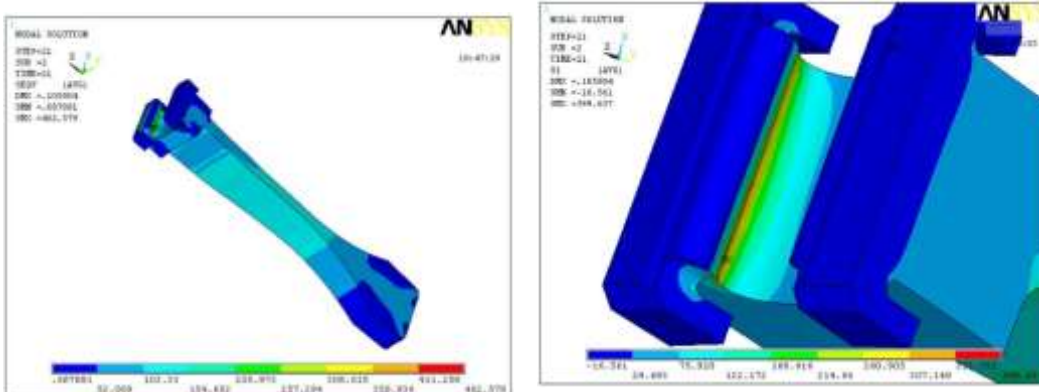
**Fig.5.13 variation of Radial and Total Deflection of Disc due to Varying Speeds**

Fig5.9 shows that radial deflection along X-direction which signification is that the radial clearance between compressor Blade-Disc assembly and casing is (0.134 mm + 0.105166 mm =0.239165 mm) compared to the existing standard value of clearance (0.5mm)

By analyzing the deformation distribution in the compressor blade and disk assembly. Here radial clearance is that “clearance between compressor blade and casing of the compressor. Whenever deflection starts radial clearance between compressor blade and casing reduce.

The main observation is that analyzing deflection from Table 5.3 and Fig 5.13, The Optimum value of Radial and Total deflection is well below the standard value, so whole compressor is safe from the radial deflection in compressor Disc. If exceed the standard value, again repeat the same analysis by having different loads. The following Table 5.1 and Fig 5.13 shows the variation of Radial as well as Total Deflection for various Centrifugal Loads.

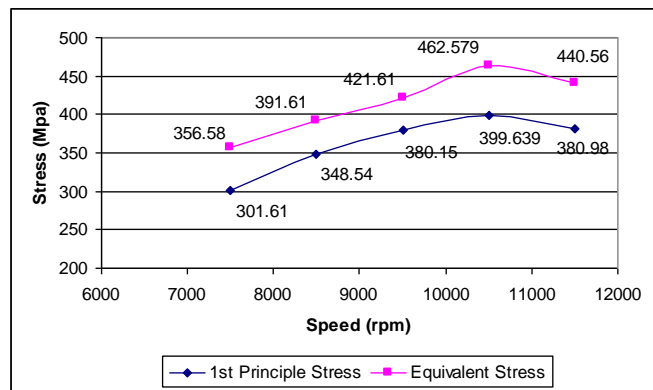
### 5.4 Typical Stress distribution results in the ROTOR DISC



**Fig.5.14 Equivalent stress distribution along xyz direction Fig.5.15 First principal stress along x- direction**

**Table.5.4 Stresses in Disc due to varying Speeds**

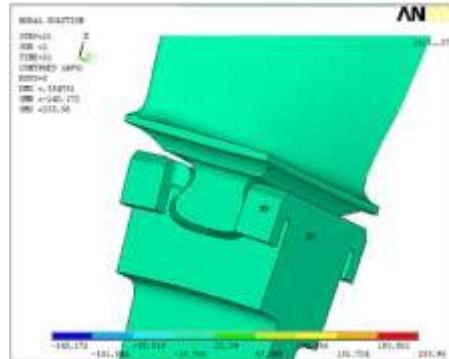
Speed (rpm)	1 <sup>st</sup> Principal Stress (Mpa)	Equivalent Stress (Mpa)
7500	301.61	356.58
8500	348.54	391.61
9500	380.15	421.61
10500	399.639	462.579
11500	380.98	440.56



**Fig.5.16 Variation of Stresses in Disc due to varying speeds**

From the above analysis of the Compressor Disc maximum stresses are induced due to existence of contact between compressor blade roots and dovetail groove of the disc in a running speed of 10500rpm. The main observations from the analysis are Equivalent stresses and 1st Principle Stresses are effectively compared with the standard material yield strength (970mpa, material property). At the maximum running speed of 10500rpm the stress values are within the standard limit, which indicates the disc is free from crack. But when the speed is increased to 11500rpm we can observe the decrease in the stress values as shown in fig.5.16. Which indicates the initiation of crack at the contact region of Blade and Disc assembly, which in turn leads to the failure if the material.

### 5.5 Contact Pressure Distribution in compressor blade and disc



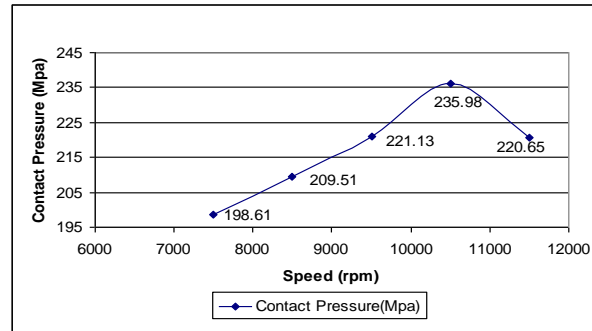
**Fig.5.17 Contact Pressure Distribution of Assembly**

Contact pressure distribution in the compressor blade disc assembly formed by the pressure load applied on the blades (80N). This pressure load distributes (0.0445N/mm<sup>2</sup>) uniformly at constant rate. The above figure shows that pressure distribution of overall assembly.

**Table.5.5 Contact Pressure distribution due to varying Speeds**

Speed(rpm)	Contact Pressure(Mpa)
7500	198.61
8500	209.51
9500	221.13
10500	235.98
11500	220.65





**Fig.5.18 Variation of Contact Pressure due to varying speeds**

## 6. CONCLUSIONS

In the present work an attempt was made to carry out contact stress analysis of compressor blade - disc assembly for gas loads and centrifugal loads by using commercial Finite Element package ANSYS.

The three types of elements SOLID-45, CONTA-173 and TARGET-170 were used for the analysis. The contact stress of bladed disc was done for static analysis.

The following Conclusion is obtained from the analysis:

- The radial clearance between compressor blade and casing (0.134mm) compared to the existing standard value of clearance (0.5mm) by analyzing the deformation distribution in the compressor blade and disc assembly.
- Determination of yield strength (413 Mpa) and effectively compared with the input yield strength (970mpa, material property). This observation clearly shows that compressor blade and disc are in safe position from the crack initiation (breaking point) at 10500rpm.
- The peak values of compressive stresses induced in the contact region are well within the design limit.
- The peak value of von-mises stresses induced near the region of contact stresses are also well within the design limit.
- The result and summary figure shows the variation of different stresses and deformation with maximum and minimum values.

## REFERENCES

- [1] Gladwell, G.M.L., Contact Problems in the Classical Theory of Elasticity, Sijthoff and Noordhoff International Publishers. Alphen aan den Rijn. The Netherlands, 1980.
- [2] Johnson, K.L., Contact Mechanics. Cambridge University Press, Cambridge, UK, 1985.
- [3] Kalker.J.J. "A Survey of the Mechanics of Contact between Solid Bodies", Z.Angew. Math. Mech., 57.pp.T3-T17, 1977.
- [4] Meda.G and Sinclair .G.B. "A Survey of Some Recent papers in Contact mechanics", Report SM 96-7, Department of Mechanical Engineering, Carnegie Mellon University, Pittsburg, PA, 1996.

- [5] Boddington.P.H.B., Chen.K. And Ruiz.C, “The Numerical Analysis of Dovetail Joints”, Compute Struct, 20.pp 731-735, 1985.
- [6] ANSYS personnel, ANSYS User’s Manual, Revision 5.2, Vol.1, ANSYS inc., Canonsburg, A, 1995.
- [7] Kenny.B.Patterson, E.A.Said and Aradhya.K.S.S, 1991, “Contact Stress Distributions in a Turbine Disk Dovetail Type Joint- A Comparison of Photoelastic and Finite Element Results.” Strain, 27.pp. 21-24.
- [8] Papanikos.P and Meguid.S.A and Stjepanovic Z., “Three-Dimensional Non-linear Finite Element Analysis of Dovetail Joints in Aeroengine Discs.” Finite Element Analysis Design.29.pp.173-186., 1998.
- [9] Hertz.H. “Miscellaneous Papers by H.Hertz”, (an English translational of Hertz’s theory) Jones and School, London, pp 146, 1986.
- [10] Thomas.H.R and Hoersch.V.A.”Stress due to Pressure of one Elastic Solid upon Another”, University of Illi.Engg.Expt.Station, Bulletin No. 212, July 1930.
- [11] Dundrus.J and Stippes.M, “Role of Elastic Constants in Certain Contact Problems”, Jl. Of App. Mech. Trans., Vol.37, pp 965-970(1970).
- [12] Srinath.L.S and Nayak.L, “Effects of Elastic Constants in Contact Stress Problems and Development of Transitional Formulae from Model to Prototype”. Mtech. Kanpur (India), (May1977).
- [13] Srinath.L.S and K.S.S. Aradhya, “Analysis of a Line Contact Problem Using Scattered Light Photoelasticity”, Proceedings of the Tenth Canadian Congress of Applied Mechanics, The University of Western Ontario, London, June1985.
- [14] Mangesh.C.Nadkarni, K.S.Shivakumar Aradhya, “On the Influence of Elastic Constants in a Line Contact Problem”, Proceedings of Natcon. ME-2004, Design group.
- [15] G.B.Sinclair, N.G.Cormier, J.H.Griffin, G.Meda,”Contact Stresses in Dovetail Attachments: Finite Element Modeling”. Journal of Eng. For Gas Turbines and Power, Vol.124, Jan-2002.